

Perception: Inference, Priors and Codes

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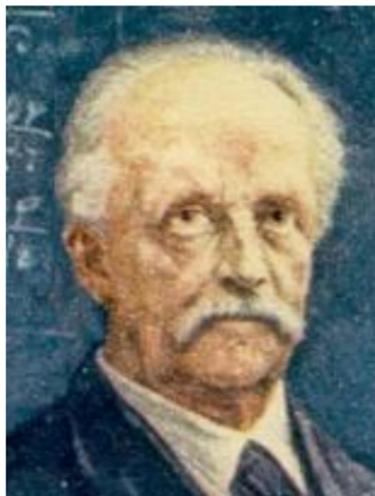
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Presumably all of the above, but there is useful intermediate abstraction.

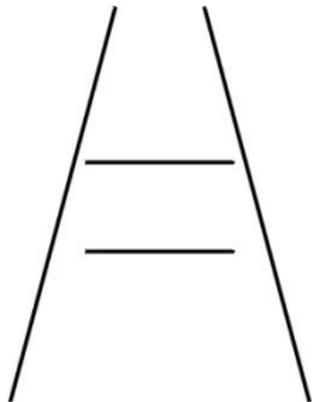
- *work out what's "out there"*.

Helmholtz

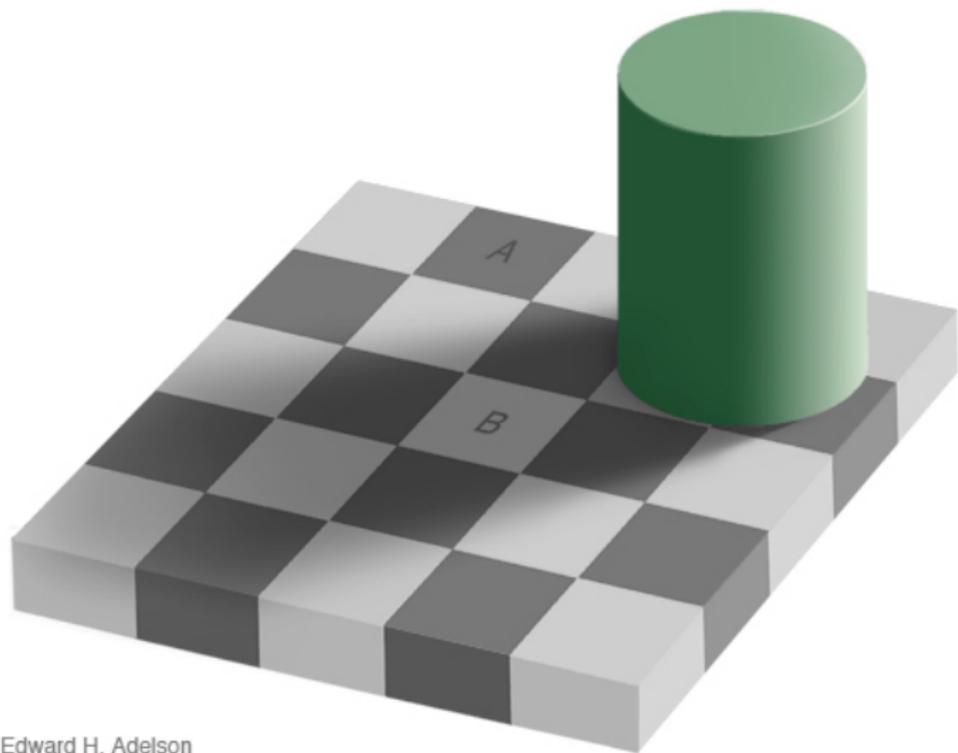


*What information, then, can the qualities of such sensations give us about the characteristics of the external causes and influences which produce them? Only this: our sensations are **signs, not images**, of such characteristics.*

Illusions

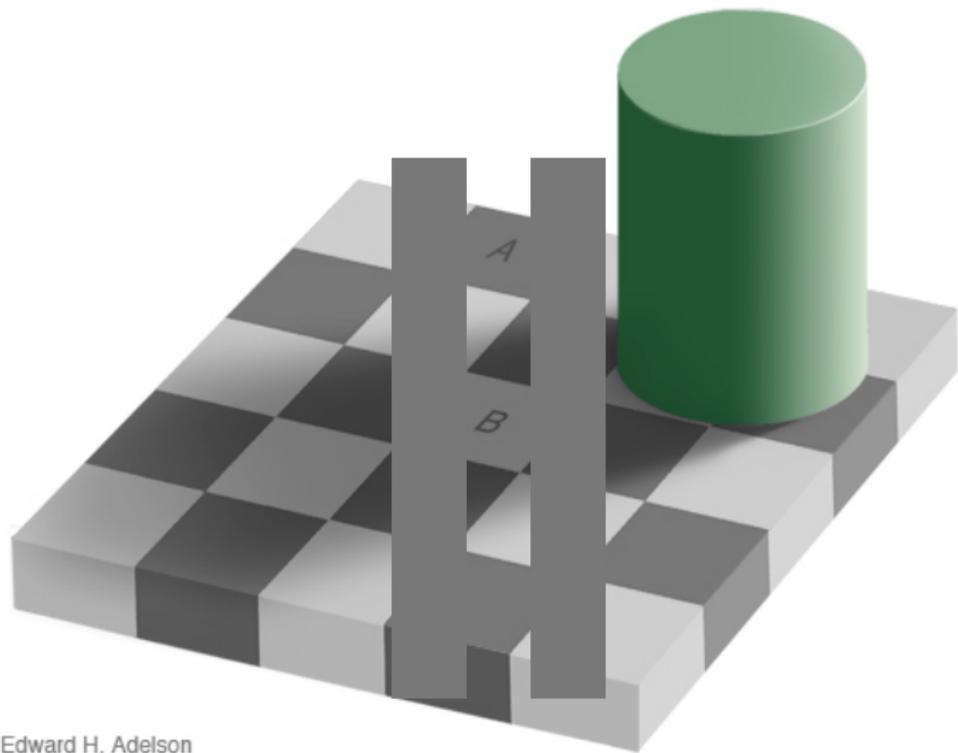


Illusions



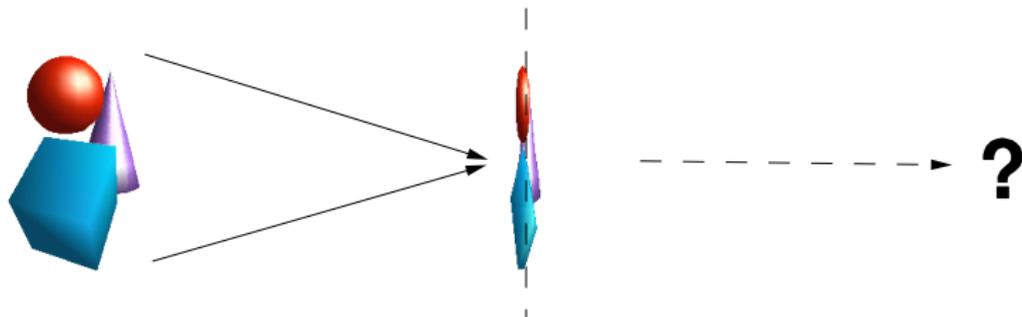
Edward H. Adelson

Illusions



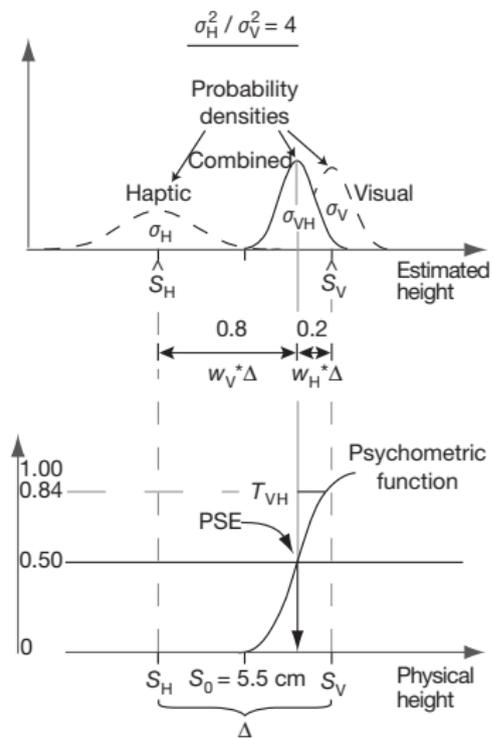
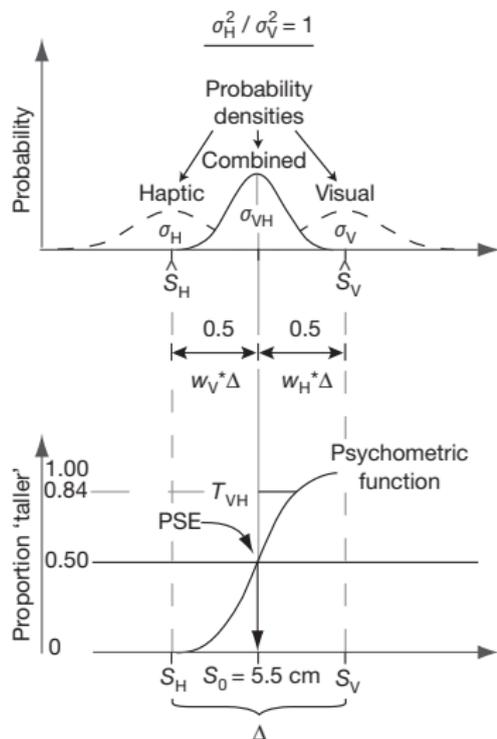
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Perception and Generative Models

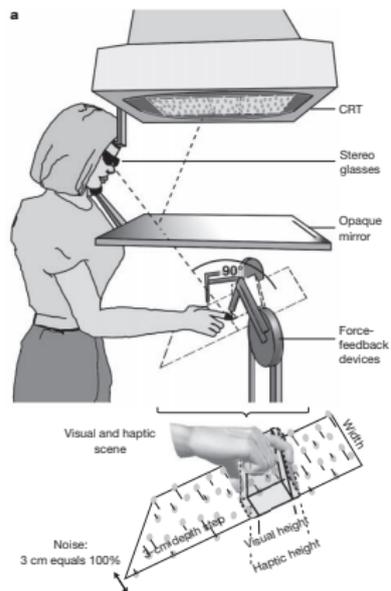


- Sensor activations reflect the state of the world through a (usually non-invertible and noisy) physical transformation.
- The goal of perception is to invert this transformation as best as possible: to **infer** the state of the world from the sensor signals.
- To do this, we need to know something about the forward (generative) process: both the transformation and the statistics of the world
- ... and to use every available source of information.

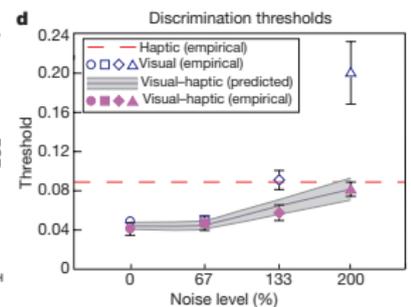
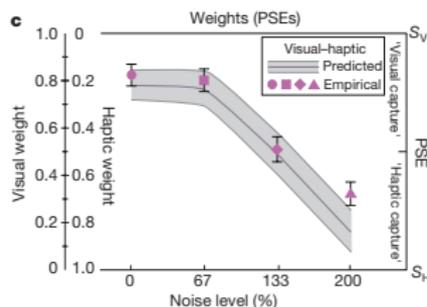
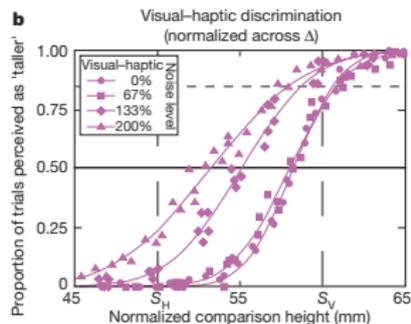
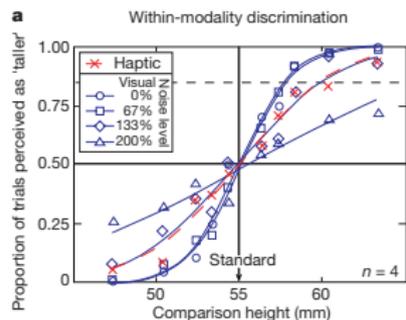
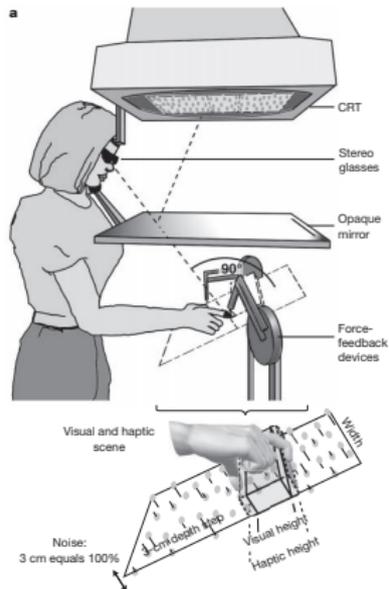
Cue combination



Cue combination



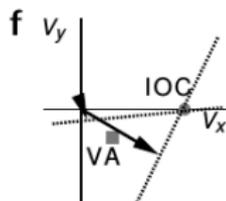
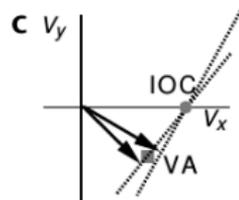
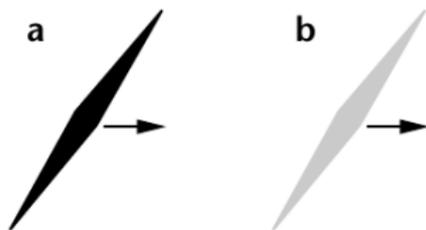
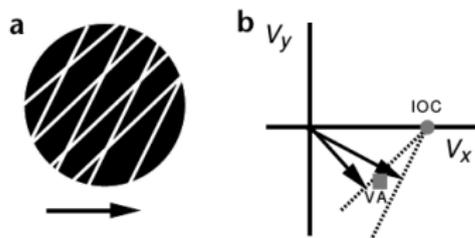
Cue combination



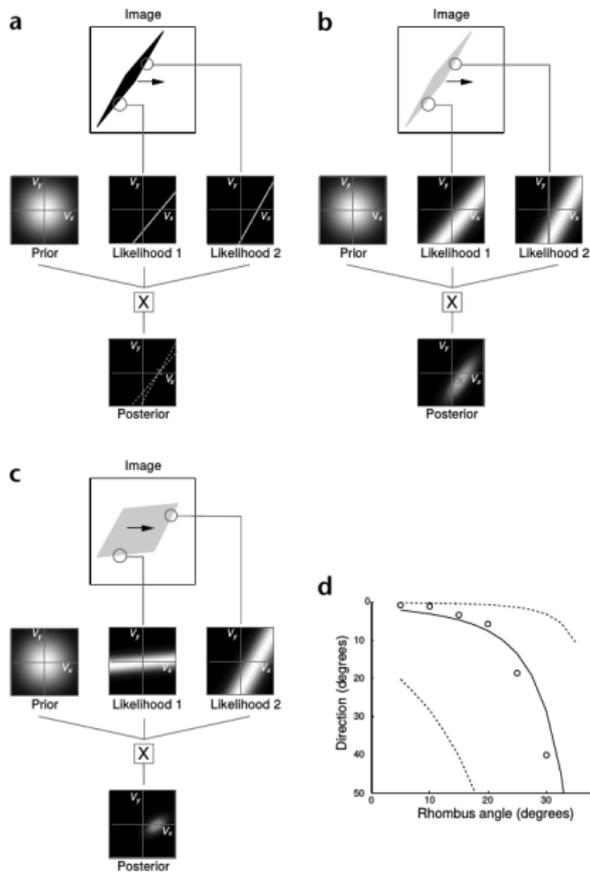
Incorporating priors – long-term priors

<https://www.cs.huji.ac.il/~yweiss/Rhombus/rhombus.html>

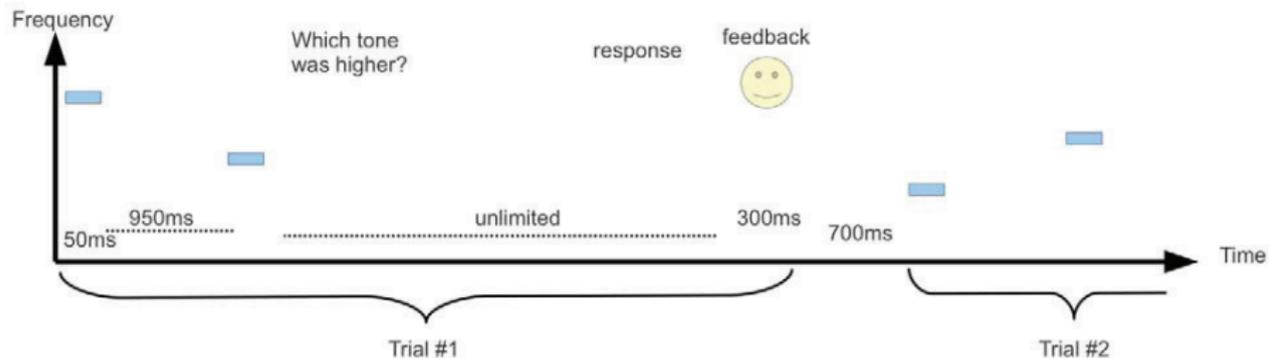
No simple rule



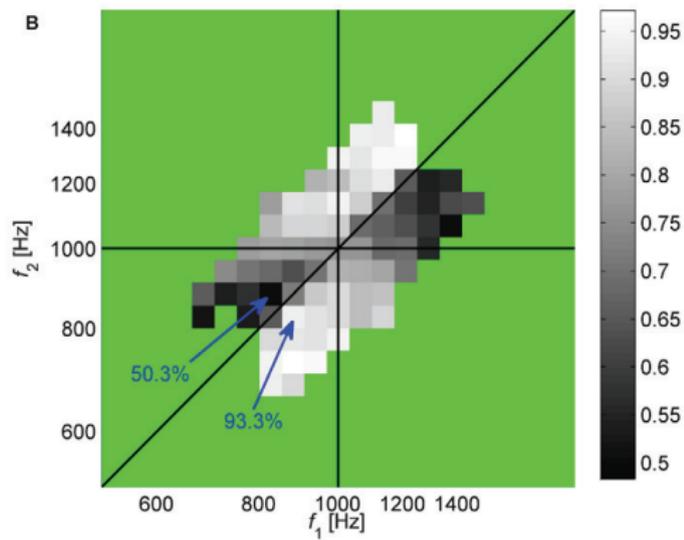
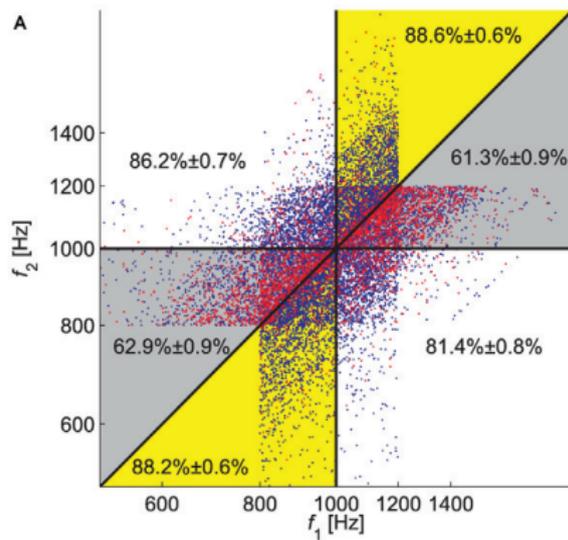
Bayesian inference under a 'slow' prior



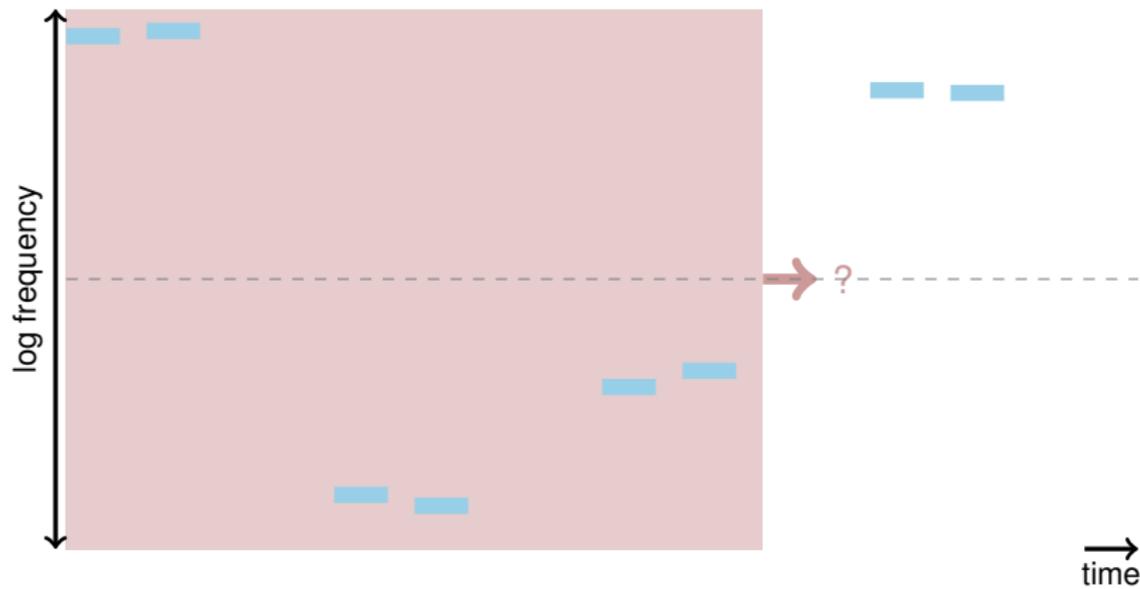
Incorporating priors – short-term adaptation



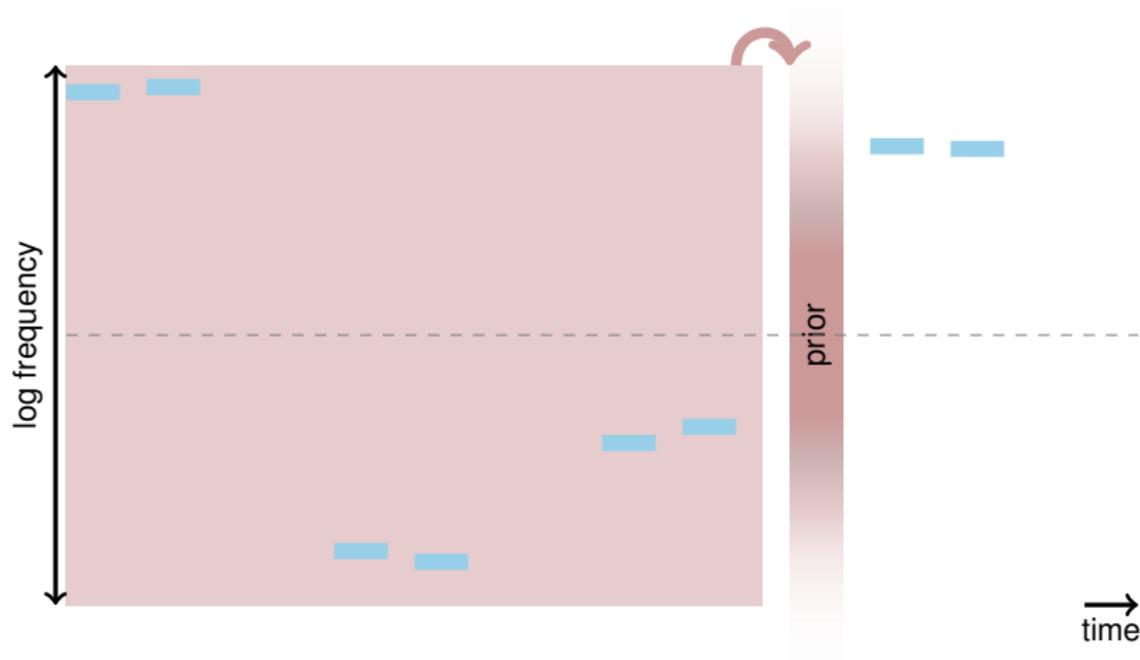
Frequency discrimination – contraction bias



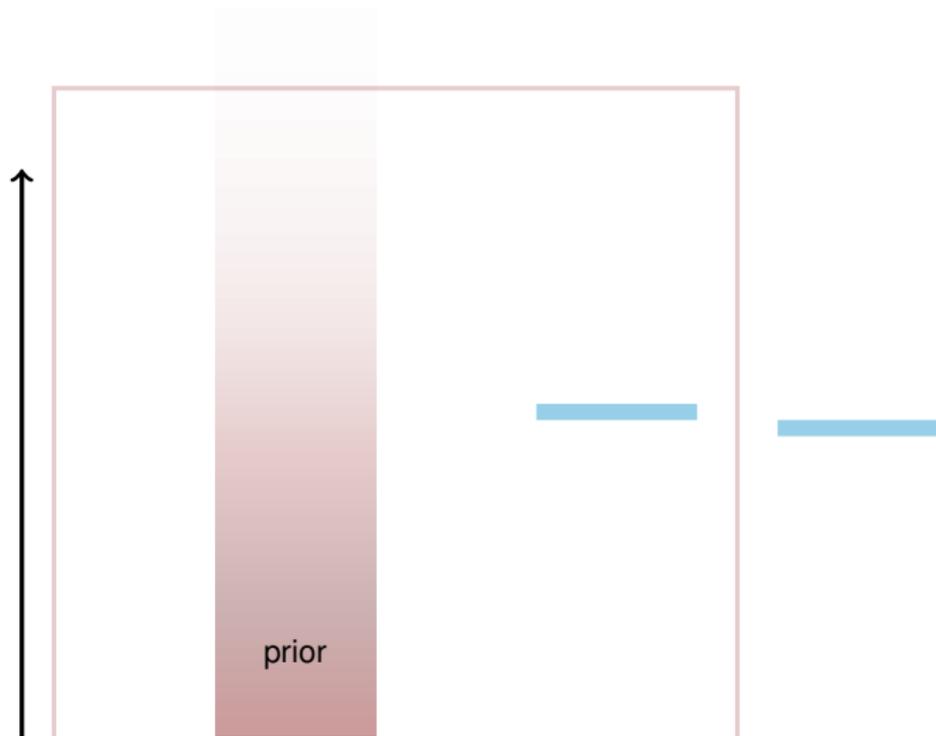
Prior context



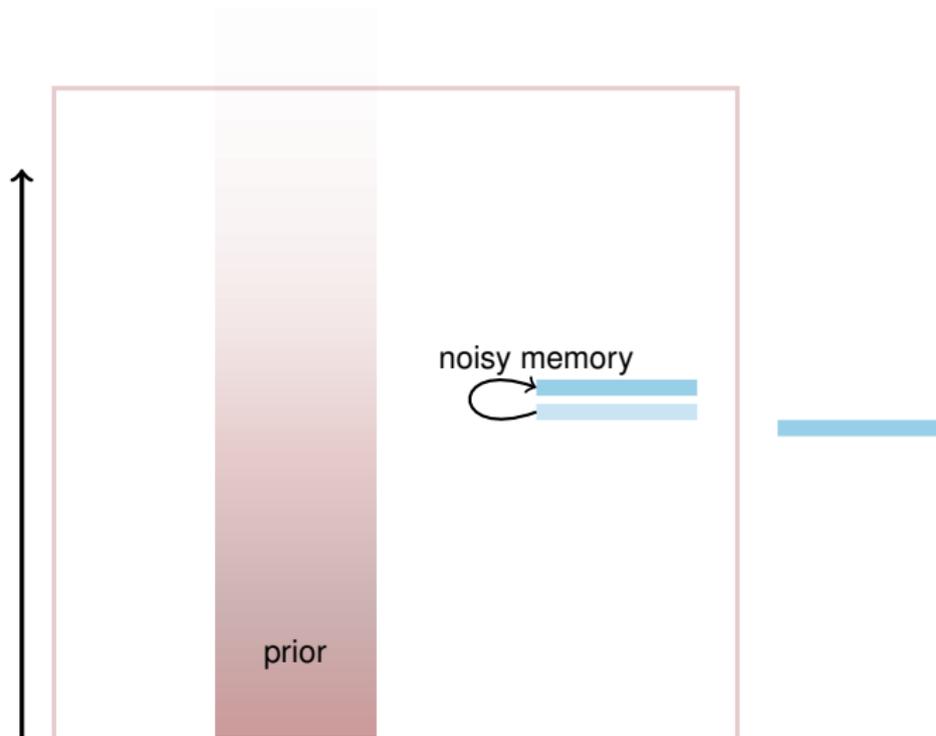
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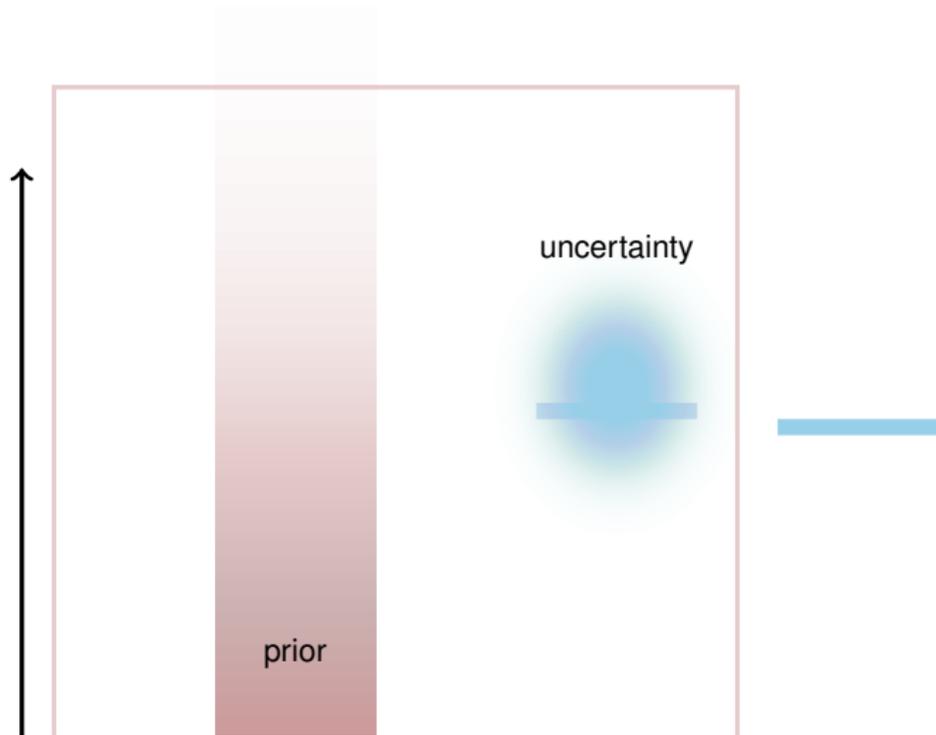
Memory



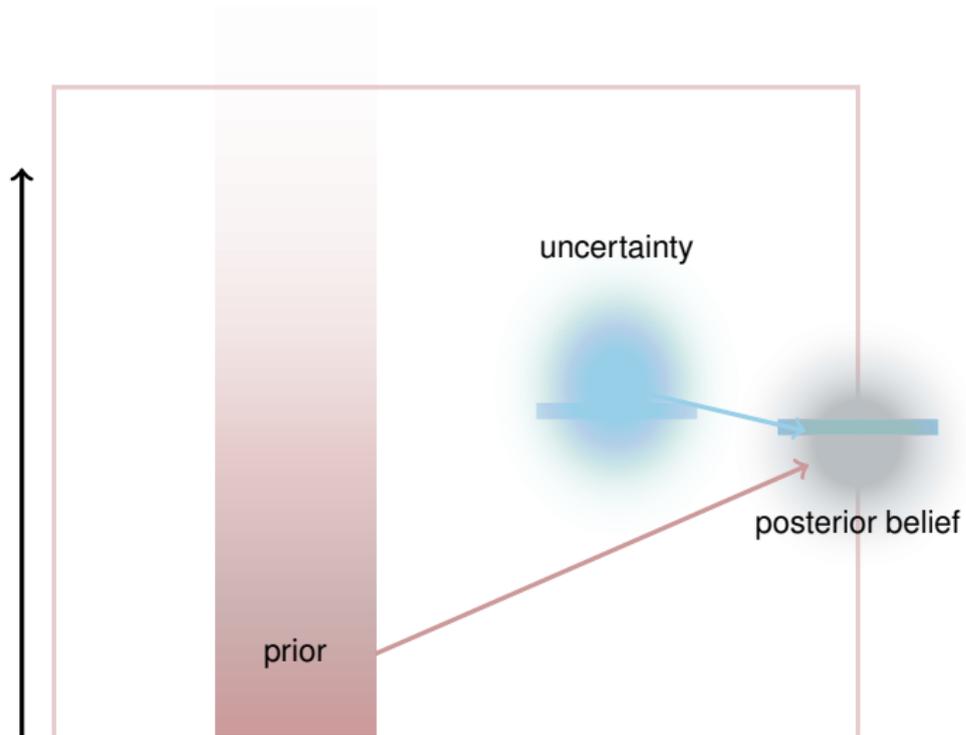
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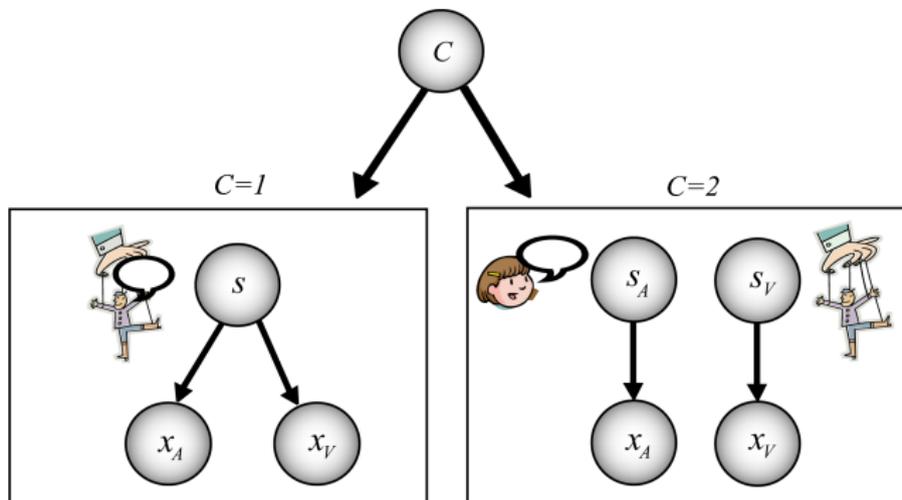
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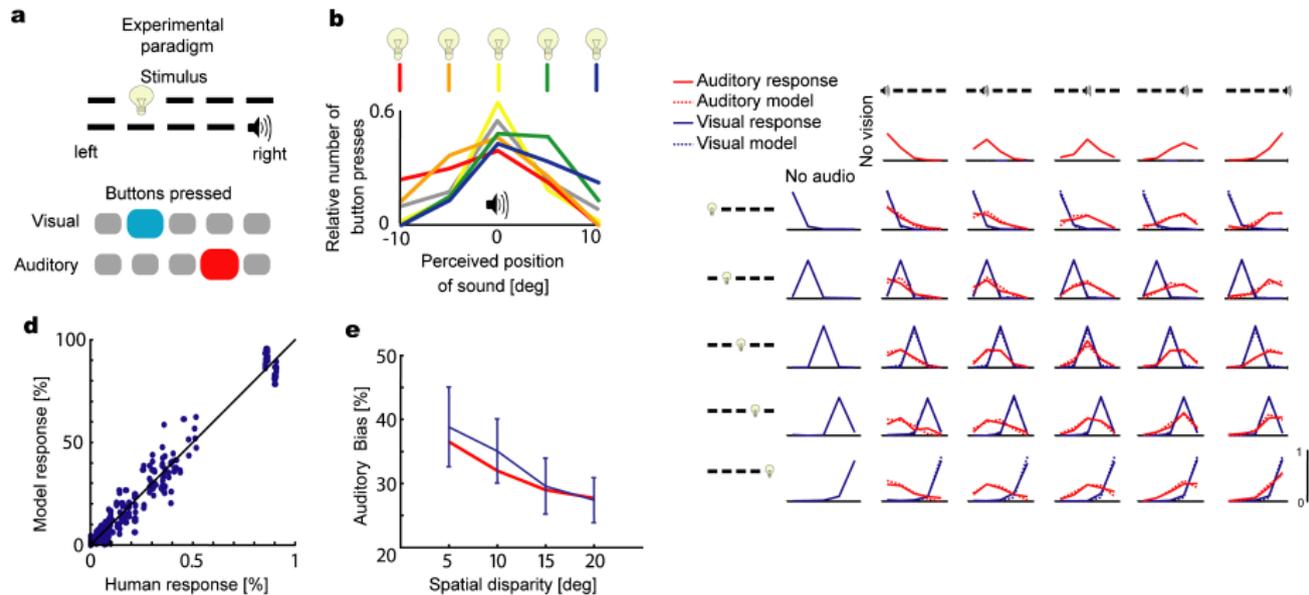
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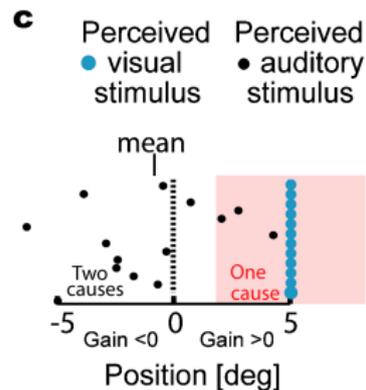
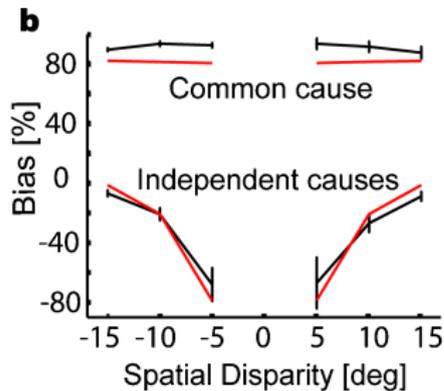
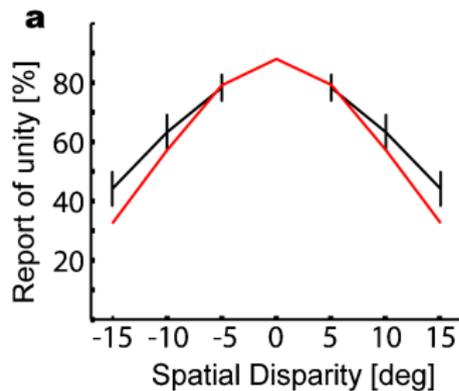
Structured inference



Structured inference



Structured inference



Some neural consequences (in theory)

- *Sensory* systems (possibly for low-level control) should feed into *Perceptual* systems.
 - See Goodale & Milner on (visual) ventral and dorsal streams.
- Response properties and receptive fields in the perceptual pathway reflect properties of elements within an inferential system.
 - We should be able to predict those properties by fitting generative models to data.
 - Representations should to represent and manipulate uncertainties, priors and other elements of inference.

Physical vs. Generic Models

- If the physics is known and simple (or if evolution is lucky), it may be possible to invert the exact physical model. This will give the most accurate results.
 - Often difficult, particularly from an evolutionary standpoint.
 - Not flexible (e.g. if the statistics of the world change).
 - May be difficult to invert.
 - Neocortex appears to be generic.
- We consider the case where a **generic** generative model, with only some elements of physicality, is adapted through **learning** to describe the generative process in the world.

Inference and Learning

Latent variable model:

$$P_{\theta}(\mathbf{y}_i) = \int d\mathbf{x} P_{\theta}(\mathbf{y}_i | \mathbf{x}) P_{\theta}(\mathbf{x})$$

Inference (find \mathbf{x}_i given \mathbf{y}_i and θ):

$$P_{\theta}(\mathbf{x}_i | \mathbf{y}_i) = \frac{P_{\theta}(\mathbf{y}_i | \mathbf{x}_i) P_{\theta}(\mathbf{x}_i)}{P_{\theta}(\mathbf{y}_i)}$$

Learning (find θ given $\{\mathbf{y}\}$)

$$P(\theta | \{\mathbf{y}\}) \propto \prod_i P_{\theta}(\mathbf{y}_i) P(\theta)$$

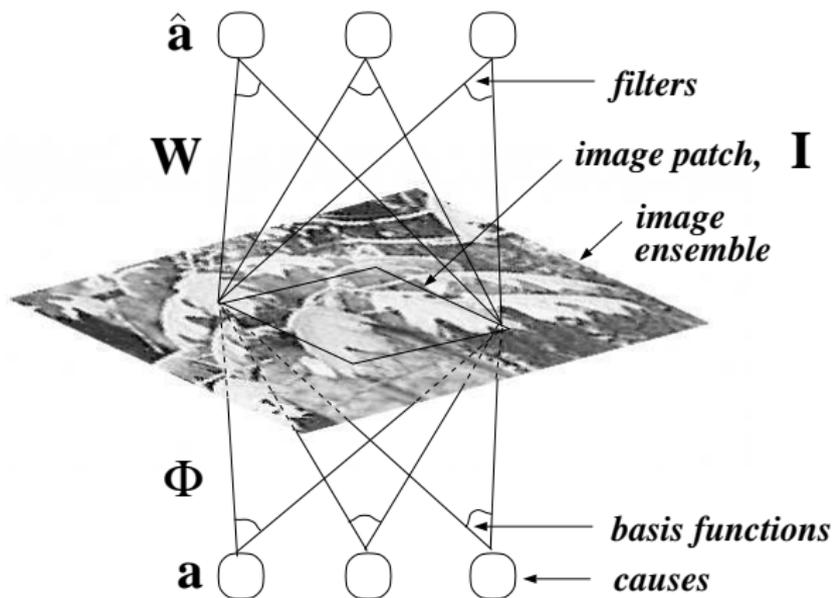
usually by ML approximation

$$\theta^* = \operatorname{argmax}_{\theta} \prod_i P_{\theta}(\mathbf{y}_i)$$

Unsupervised Learning

- Even if the ultimate goal is supervised or reinforcement learning, unsupervised learning can serve as a useful “front end” for finding good representations.
- Generative models provide an extremely successful framework for unsupervised learning.
- Other viewpoints, such as redundancy reduction, can be viewed as special cases of the generative modelling approach.

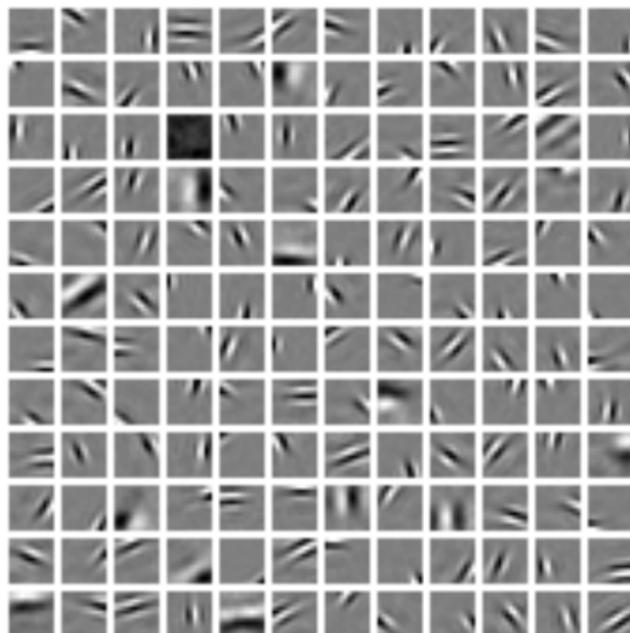
Linear Image Codes



Sparse Coding

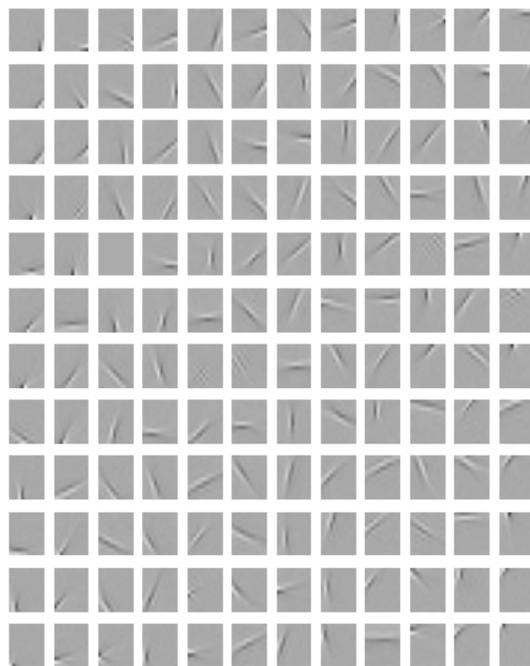
$$E = \min_{\{a_i\}} \sum_{x,y} \underbrace{\left[I(x,y) - \sum_i a_i \phi_i(x,y) \right]^2}_{\log P(Y|X)} + \lambda \underbrace{\sum_i S(a_i)}_{\log P(X)}$$

$$S(a) = \log(1 + (a/\sigma)^2)$$



$$E = -H \left[g \left(\sum_{x,y} W_i(x,y) I(x,y) \right) \right]$$

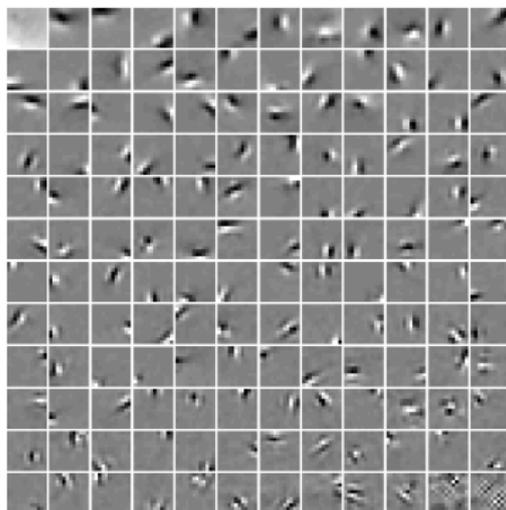
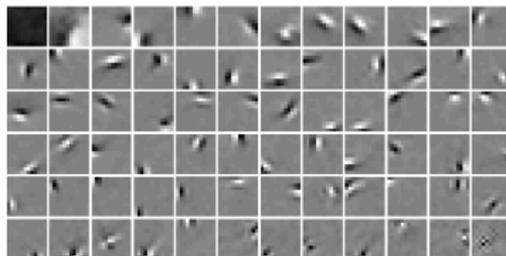
$$g(a) = \frac{1}{1 + e^{-a}}$$



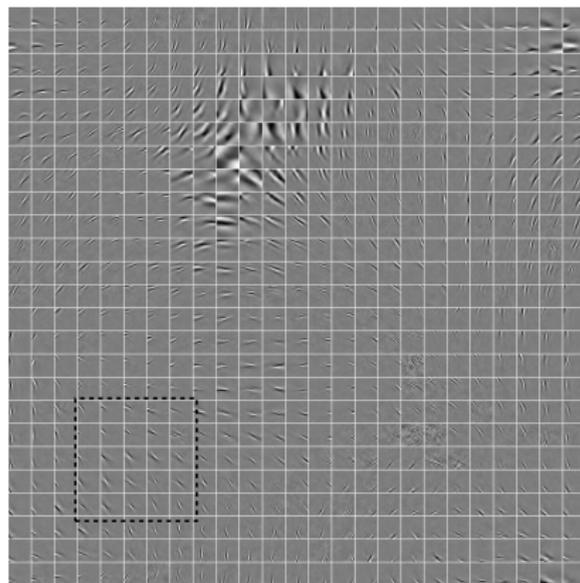
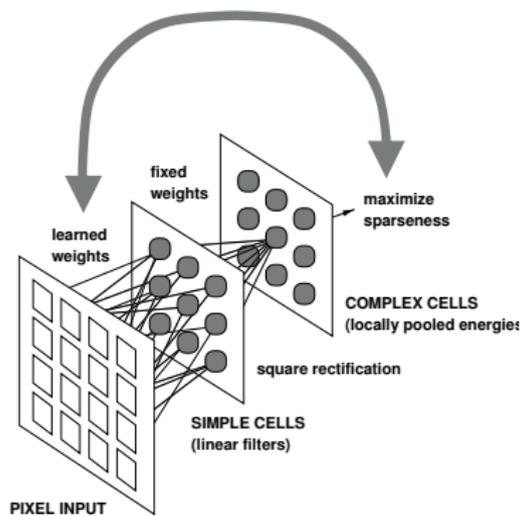
Overcompleteness

$$E = - \int d\mathbf{a} P_{\phi}(I | \mathbf{a}) P_S(\mathbf{a})$$

(Integral is approximated by saddle-point method.)

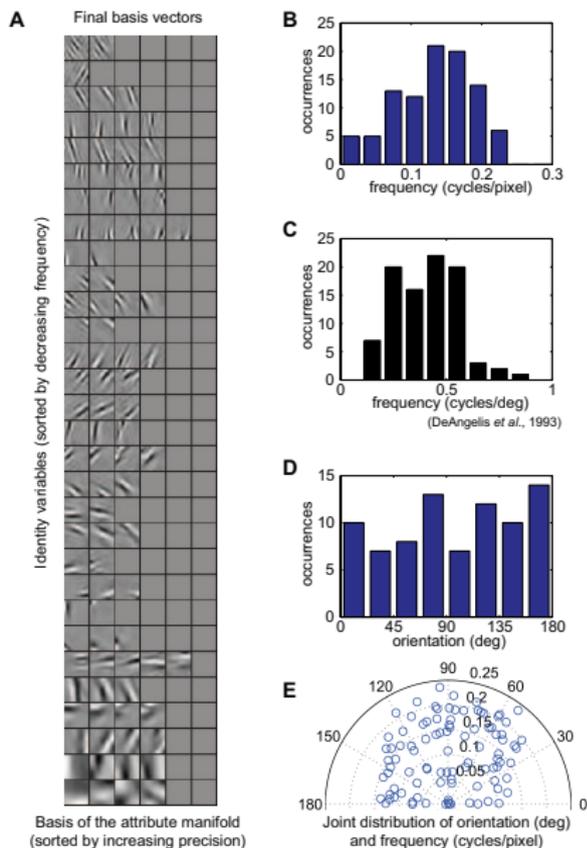


Topographic ICA - Hyvärinen & Hoyer



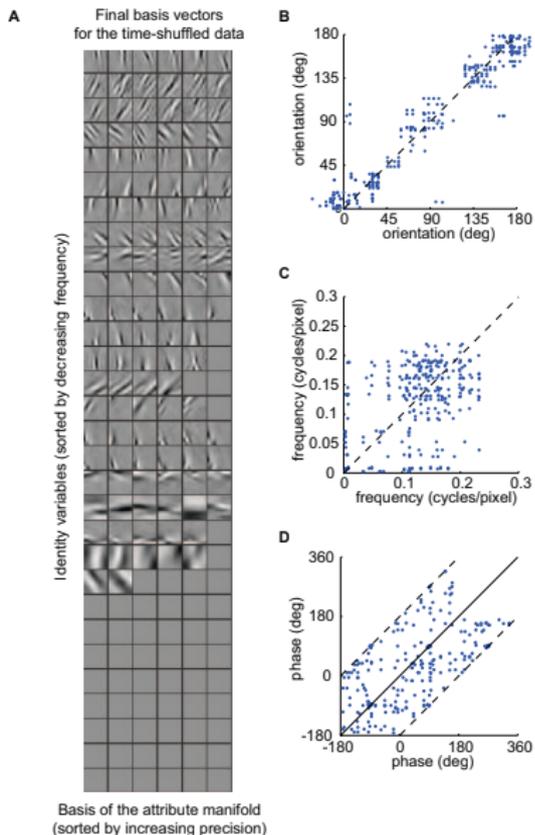
Dynamic constancy

- Dynamic images and latent variables $I(x, y, t) \Rightarrow a_i(t)$.
- Impose prior limiting change in $a_i(t)$.
- With suitably constrained models, results in phase insensitivity (complex cells).



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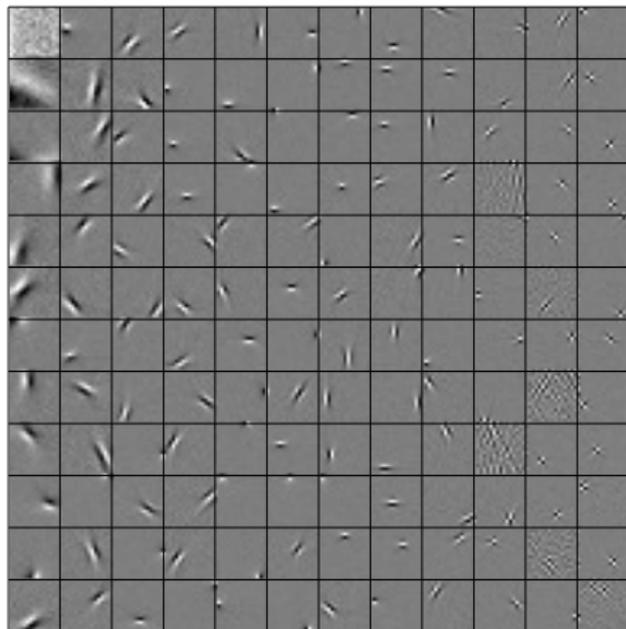


Recognition models

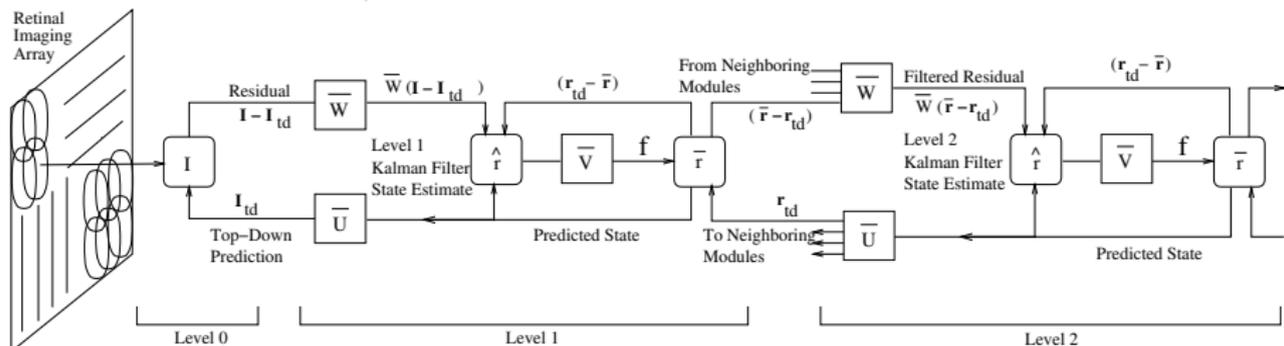
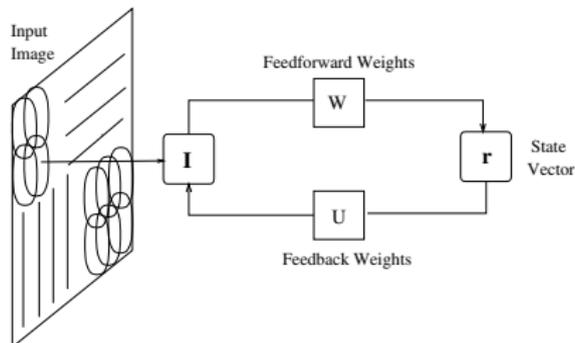
$$P(I(x, y)) = \frac{e^{-E(\hat{\mathbf{a}})}}{\int d\mathbf{b} e^{-E(\mathbf{b})}}$$

$$E(\hat{\mathbf{a}}) = - \sum_i \log P_i(\hat{a}_i)$$

$$\hat{a}_i = \sum_{x, y} W(x, y) I(x, y)$$



Feedback cancellation (or predictive coding)



Lateral normalization

